

EE 1130

Freshman Eng. Design for Electrical and Computer Eng.

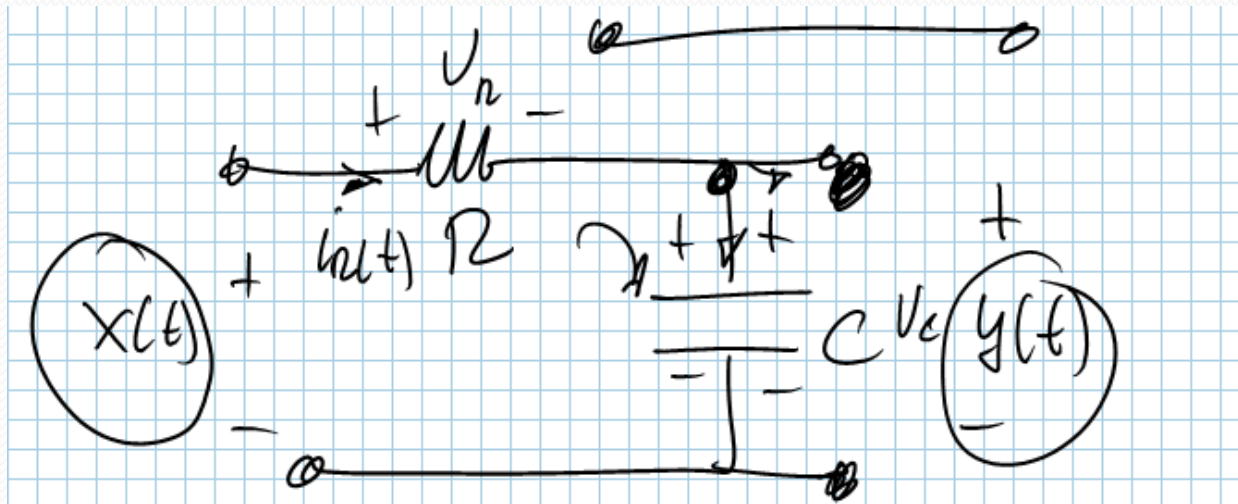
Class 3

Signal Processing Module (DSP).

- Differential Equations.
- Laplace Transform. Transfer Function.
- Simulink with Transfer Functions. Zeros, Poles.

Simulink: Differential Equations.

- Any Linear Time Invariant system could be modeled as the solution of a differential equation (DE) .
- In the case of Low Pass RC filter shown in next figure:



- The Differential Equation is:

$$RC\dot{y} + y = x$$

Simulink: Differential Equations.

- A differential equation is not instant.

$$y(t) = 2x(t)$$

- A differential equation has into account velocities!!!

$$K \frac{dy}{dt} + y(t) = 2x(t)$$

Simulink: Differential Equations.

- The circuit analysis is shown in next figure:

$$RC \frac{dy}{dt} + y(t) = x(t)$$

Simulink: Differential Equations.

$$RC\dot{y} + y = x$$

- Where y with the dot is the first derivative of $y(t)$ and x is $x(t)$. R and C are the values of the Resistor and Capacitor respectively.
- The Differential Equation could be simulated with Simulink.
- However, the Differential Equation must be modified to an Integral Equation, since integrator blocks are more used than derivative blocks.

$$\int (RC\dot{y} + y) dy = \int x dx$$

Simulink: Differential Equations.

- The integral is linear:

$$RC \int \dot{y} dt + \int y dt = \int x dt$$

$$RCy = \int x dt - \int y dt$$

$$y = \frac{1}{RC} \int (x - y) dt$$

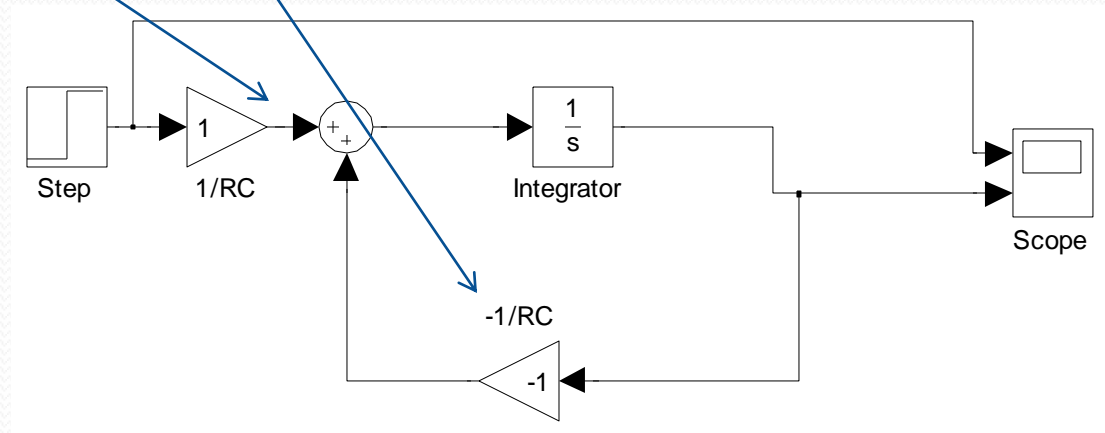
$$y = \int \left(\frac{1}{RC} x - \frac{1}{RC} y \right) dt$$

Simulink: Differential Equations.

- The block diagram could be implemented from this equation:

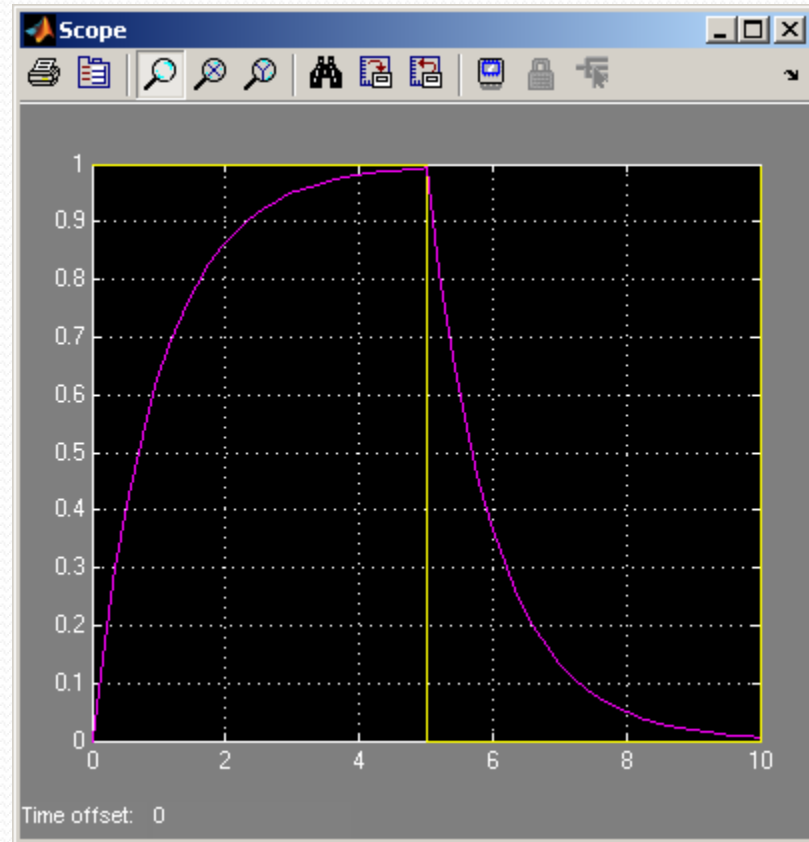
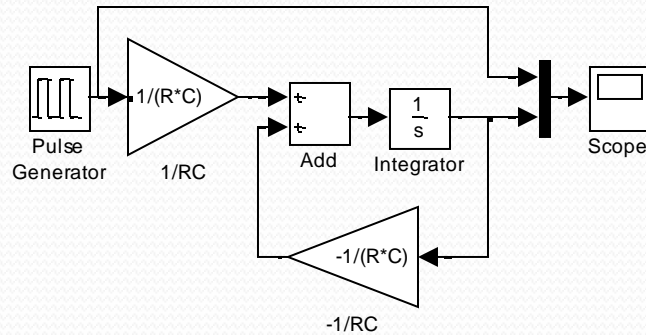
$$y = \int \left(\frac{1}{RC} x - \frac{1}{RC} y \right) dt$$

$$\frac{1}{RC} x - \frac{1}{RC} y$$



Simulink: Differential Equations.

- Lets hands on (charge and discharge):



Simulink: Laplace Transform.

- Working with DE is not easy. Laplace Transform allows avoid DE.
- Also, it allows us to have an analytic relation input/output!!

$$RC\dot{y} + y = x$$

$$RC \frac{dy}{dt} + y(t) = x(t)$$

- Applying Laplace:

$$RCsY(s) + Y(s) = X(s)$$

Simulink: Laplace Transform.

- Operating:

$$Y(s)(RCs + 1) = X(s)$$

$$Y(s) = \frac{1}{RCs + 1} X(s)$$

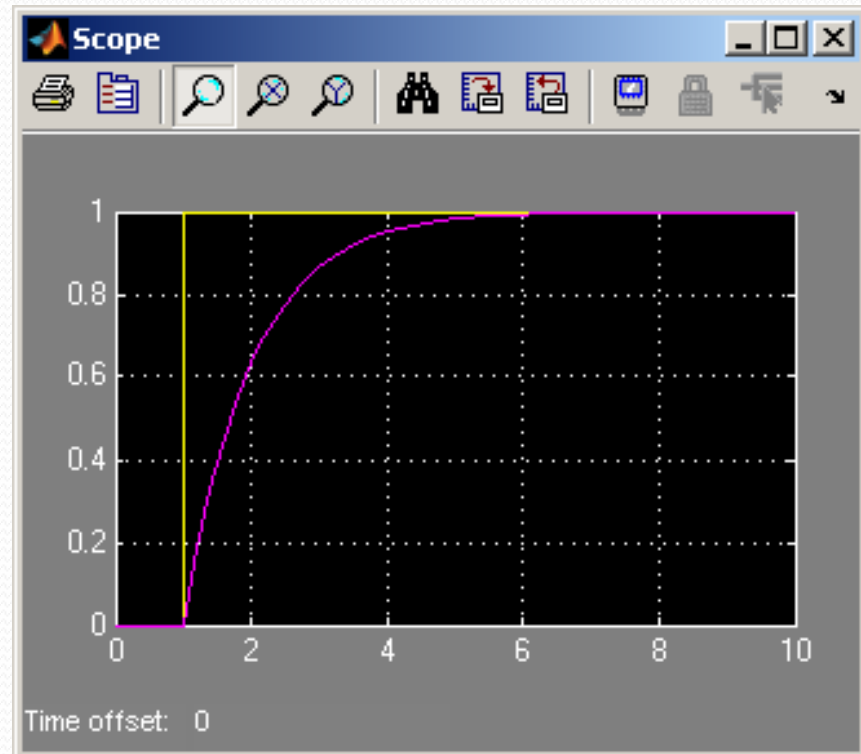
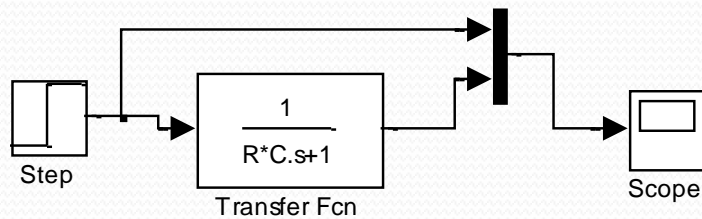
- We could easily implement this in Simulink!!!
- The multiplier of $X(s)$ is called Transfer Function.

$$H(s) = \frac{1}{RCs + 1}$$

Simulink: Laplace Transform.

- Simulating:

$$H(s) = \frac{1}{RCs + 1}$$





End of Class